

Explaining the VLBI Estimated Degree-1 Load Variation Via Atmospheric, Oceanic, and Hydrological Mass Variations

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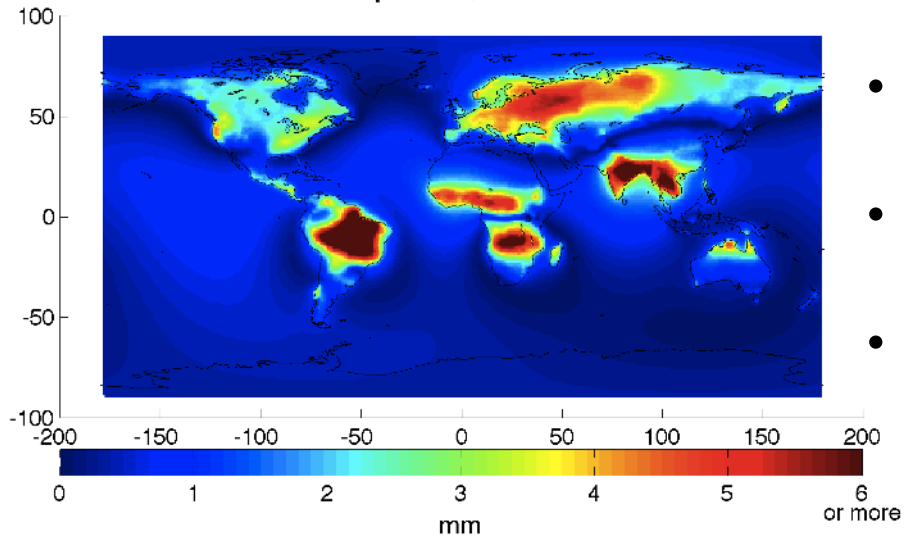
1. Hydrology Loading
2. Terrestrial Reference Frame Scale
3. Nontidal Ocean Loading
4. Loading Services at GSFC
5. Estimation of Degree-1 Deformation

Hydrology loading series calculation

- NASA GLDAS hydrology model (Rodell et al. 2004)
- Contributions from soil moisture, snow water, plant canopy surface water storage
- Used the $1^{\circ} \times 1^{\circ}$ monthly average model (1979-present)
- Site displacement loading computed by usual Green's function approach
- Vertical displacements are 3-10 mm; large annual signal

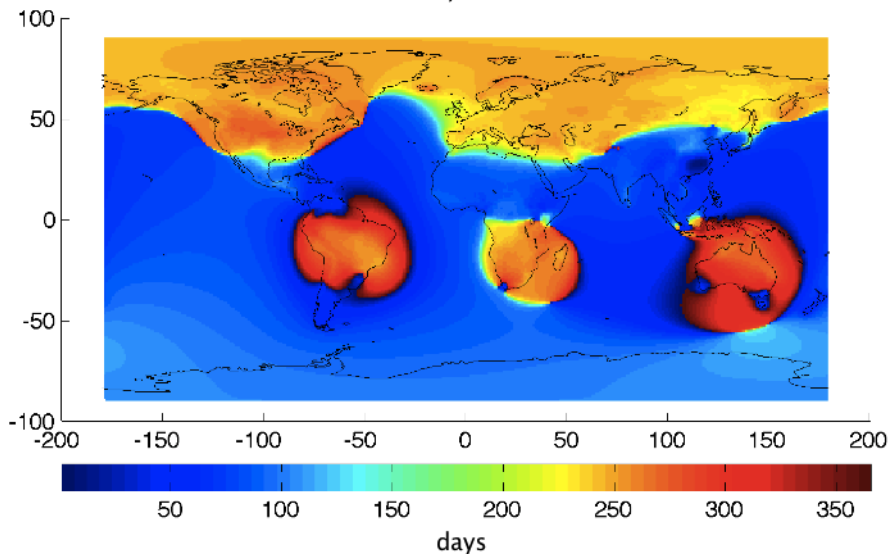
Hydrology Loading

Amplitude, GLDAS

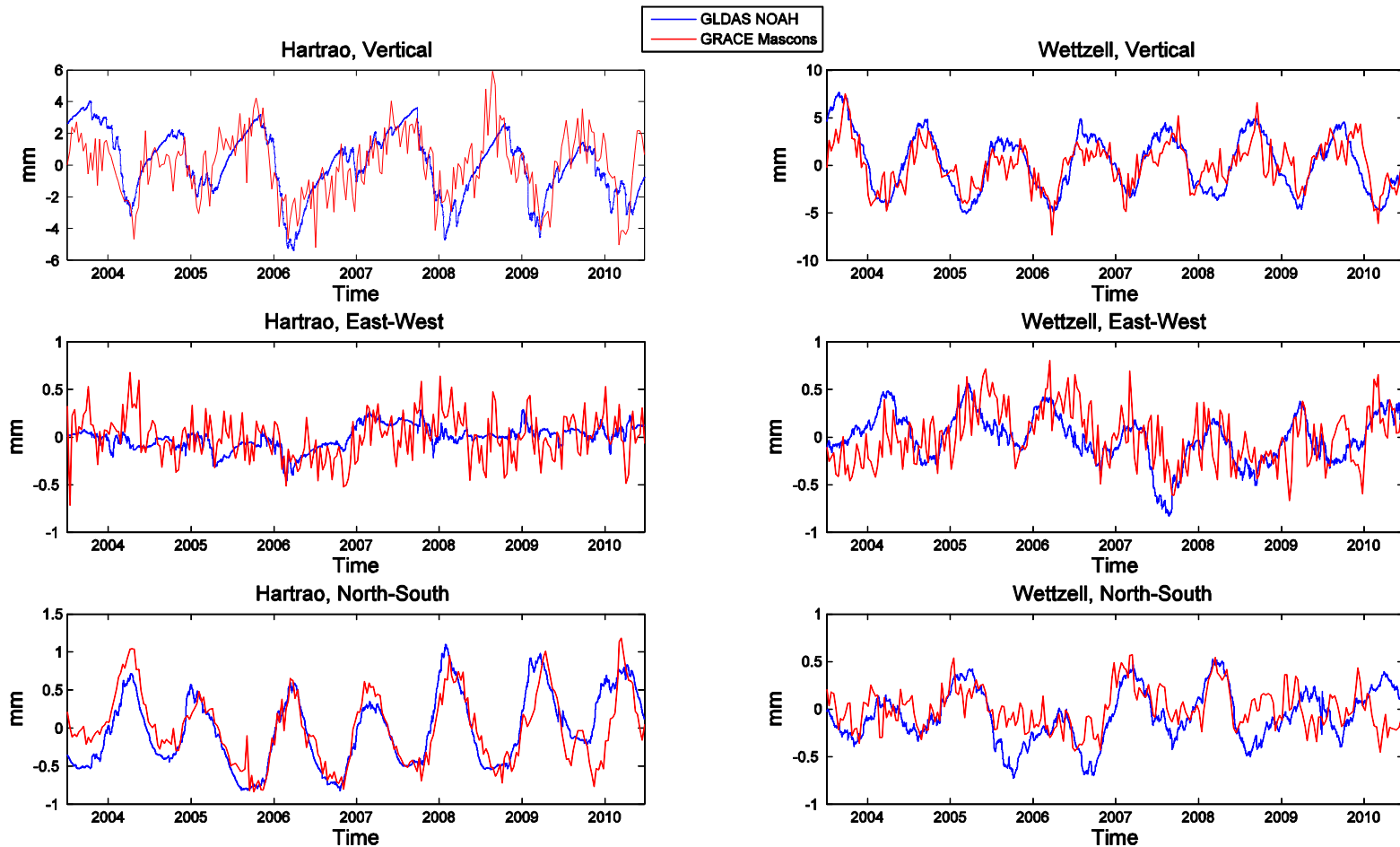


- Computed annual vertical amplitude of GLDAS loading signal
- Amplitudes from 0 to 10 mm (Amazon basin)
- Annual amplitudes for VLBI sites < 4.5 mm

Phase, GLDAS

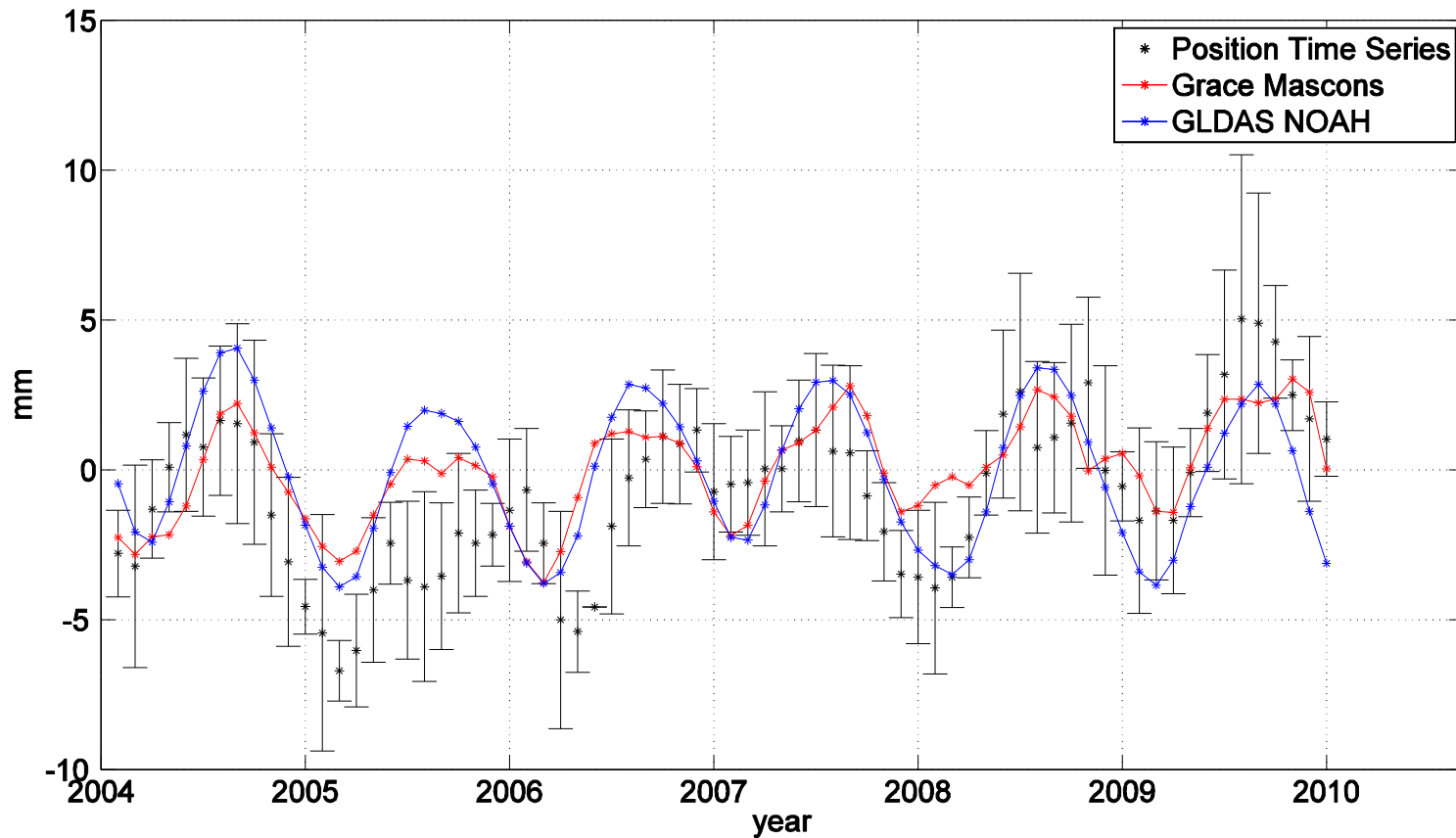


Hydrology Loading



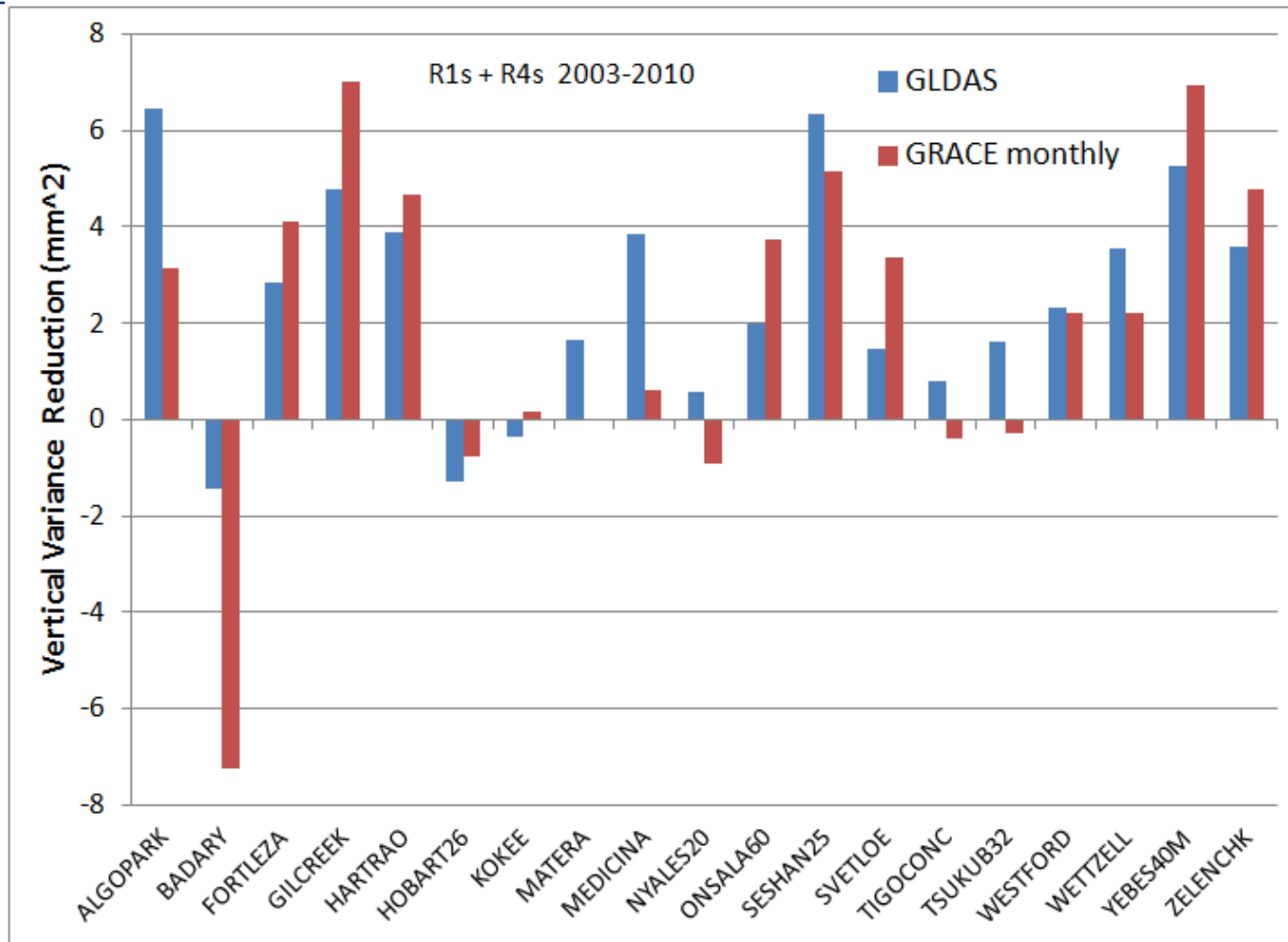
- VLBI sites: HartRAO (South Africa) and Wettzell (Germany)
- Reasonable agreement of 10-day GRACE mascon loading and GLDAS loading

Hydrology Loading

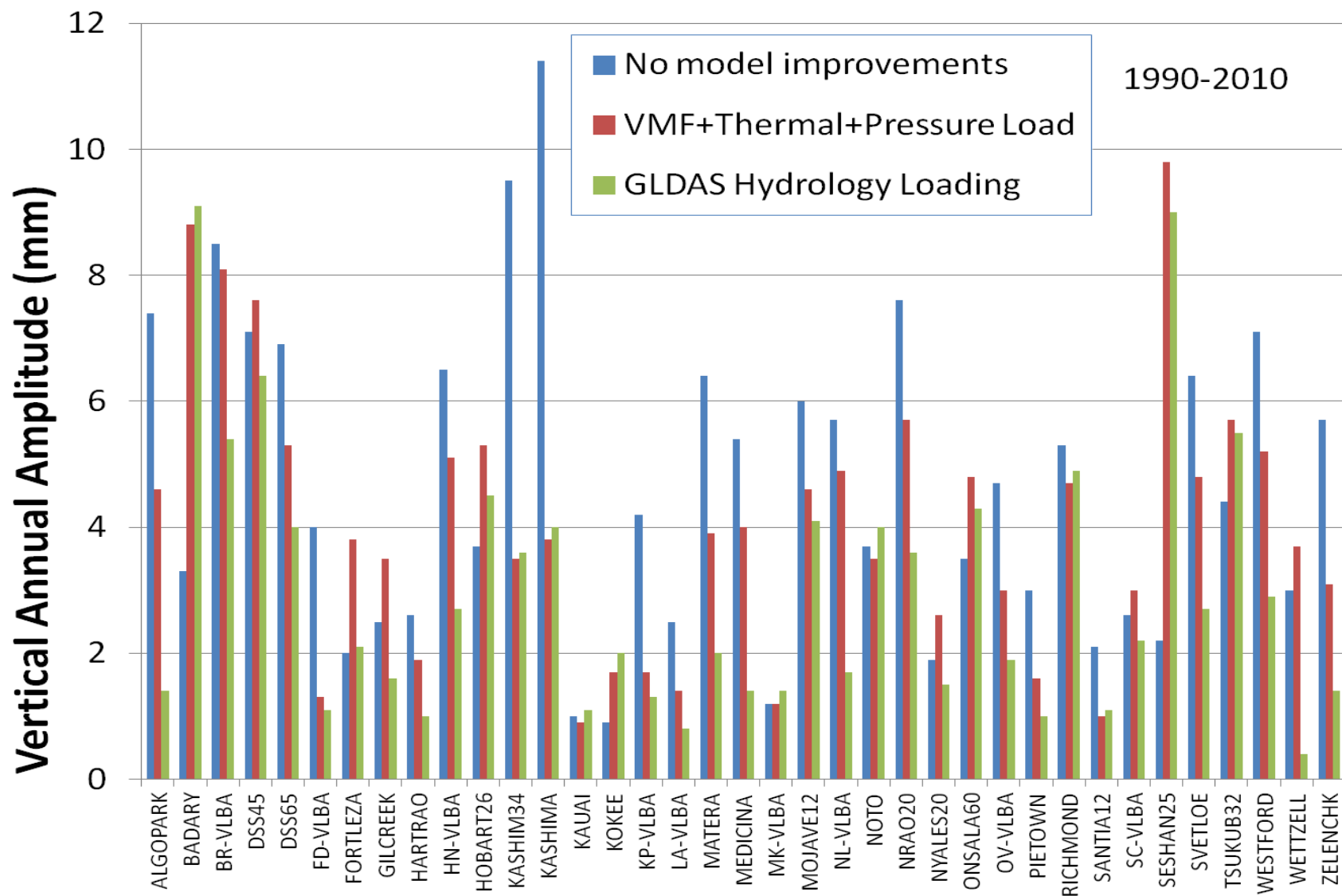


- Comparison of monthly average vertical VLBI position time series at Wettzell and the GLDAS and GRACE mascon loading series.
- Correlations between loading series and the VLBI series are 0.57(GLDAS) and 0.48(GRACE)

Hydrology Loading



- Analysis of VLBI operational weekly R1 and R4 network sessions 2003-2010
- Vertical variance is reduced with either the GLDAS or GRACE loading series



Reference Frame Scale



	Annual (ppb)		Semi-annual (ppb)	
	cos	sin	cos	sin
Base case	-0.38	-0.37	0.05	0.20
+VMF1+Thermal Def	-0.16	-0.31		
+Atmospheric Load	-0.19	-0.33		
+Hydrologic Load	-0.06	-0.06	-0.01	0.08

Uncertainties = 0.02 ppb

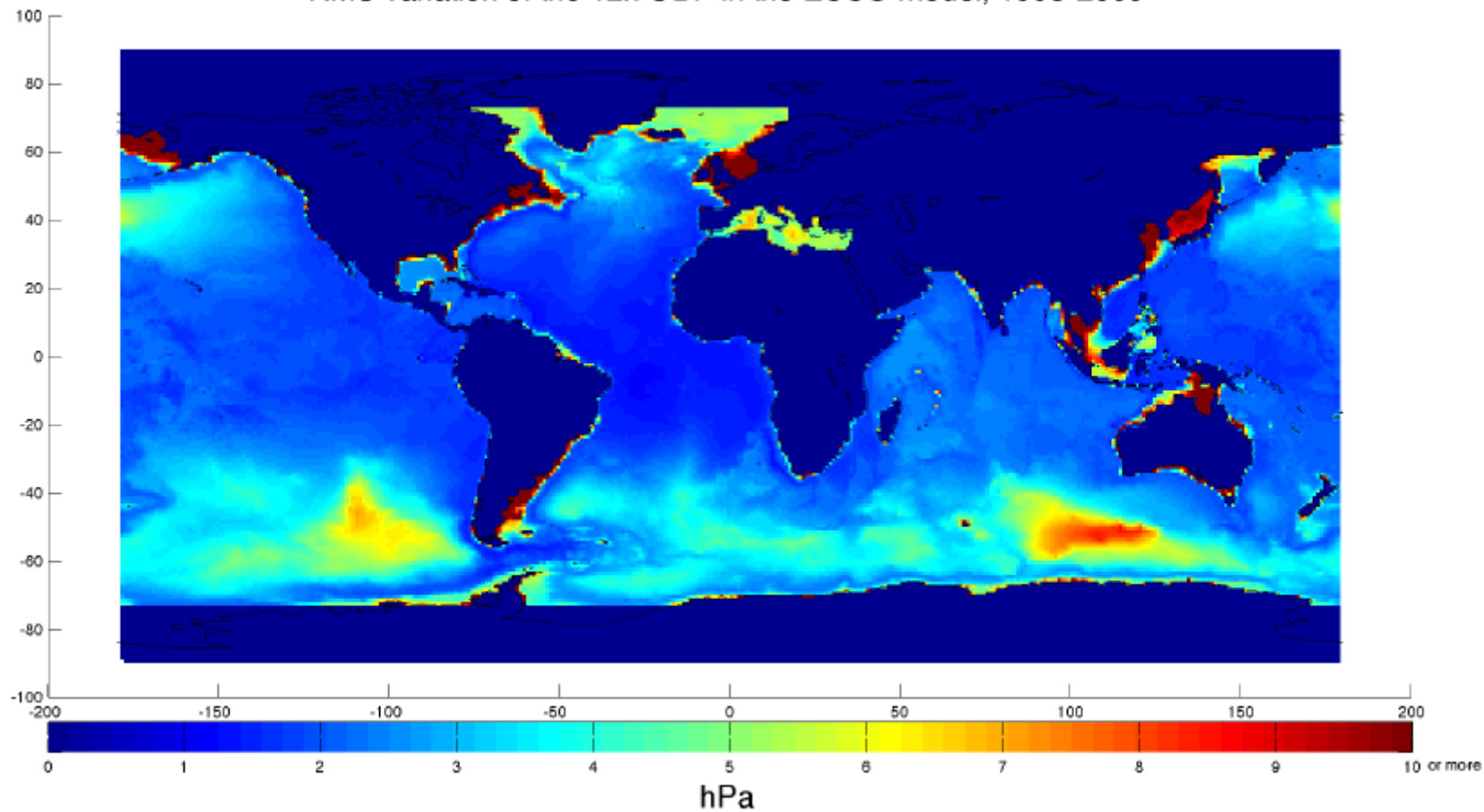
- For the base case, the NMF mapping function was used and no pressure loading was applied
- The biggest reduction in annual amplitude is from hydrology loading

Nontidal Ocean Loading Calculation

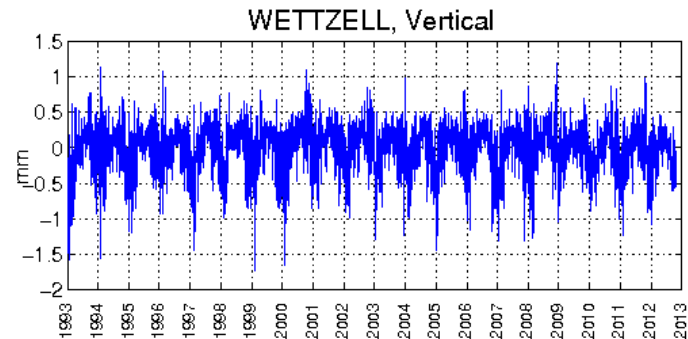
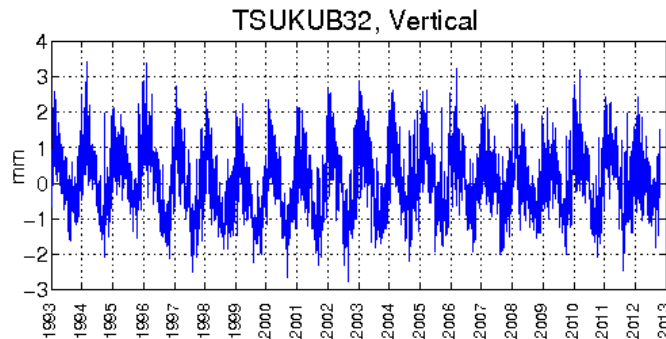
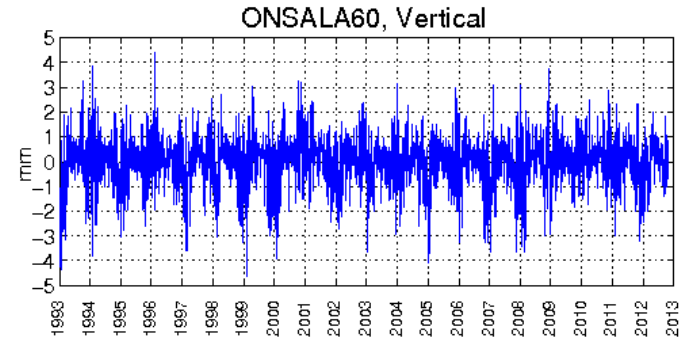
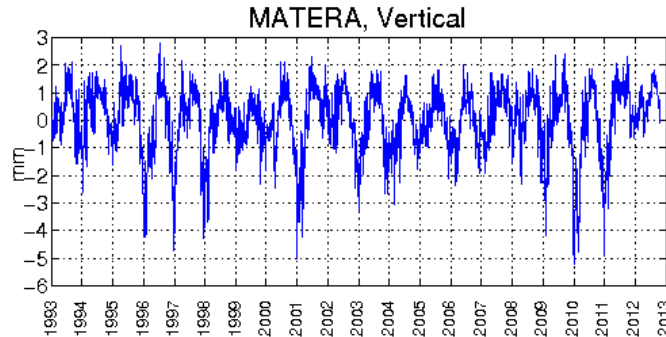
- JPL ECCO ocean model
- Used 12-hour ocean bottom pressure since 1993
- Oceanic volume (not mass) conserving
- Site displacement loading computed by usual Green's function approach
- Vertical displacements are largest near the coast; large annual signal; rms variation VLBI sites: 0.11-1.67 mm

Nontidal Ocean Loading

RMS variation of the 12h OBP in the ECCO model, 1993-2009

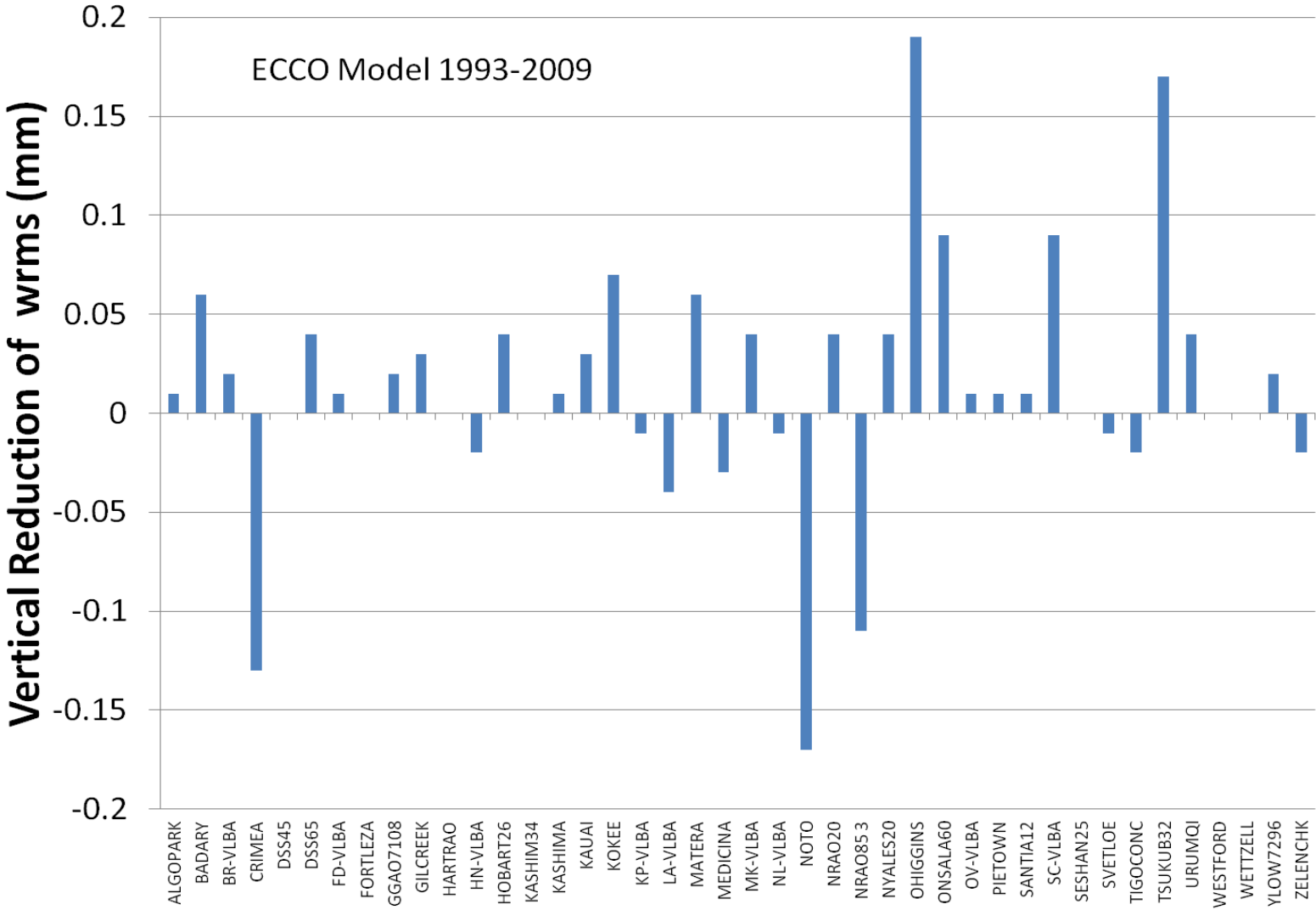


Nontidal Ocean Loading

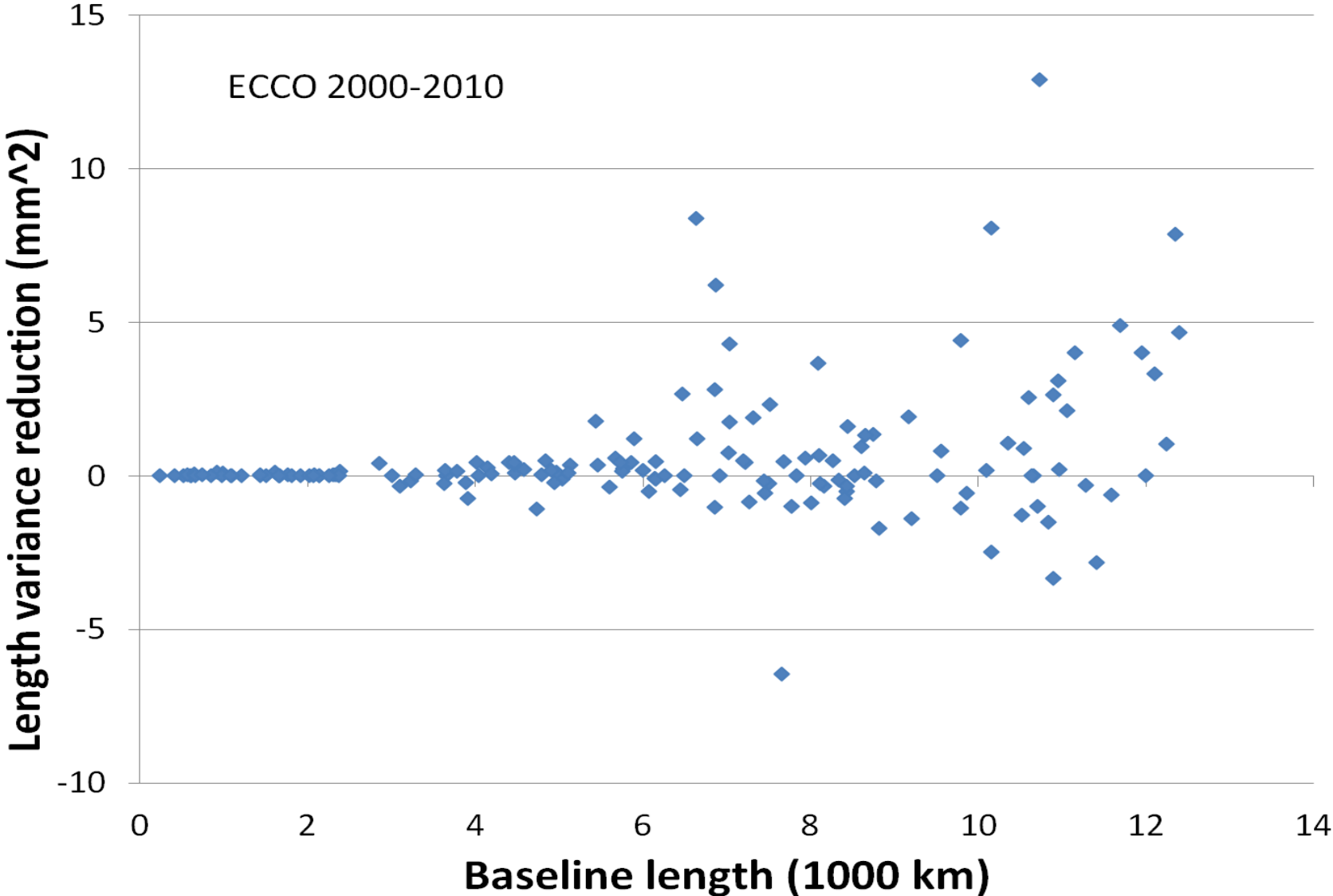


- Typical vertical loading series at VLBI sites:
Coastal sites: Matera (Italy) rms 1.18 mm, Onsala (Sweden) rms 0.85 mm, Tsukuba (Japan) rms 0.89 mm
Inland site: Wettzell (Germany) rms 0.31 mm
- RMS variation is much smaller than VLBI residual vertical RMS

Nontidal Ocean Loading

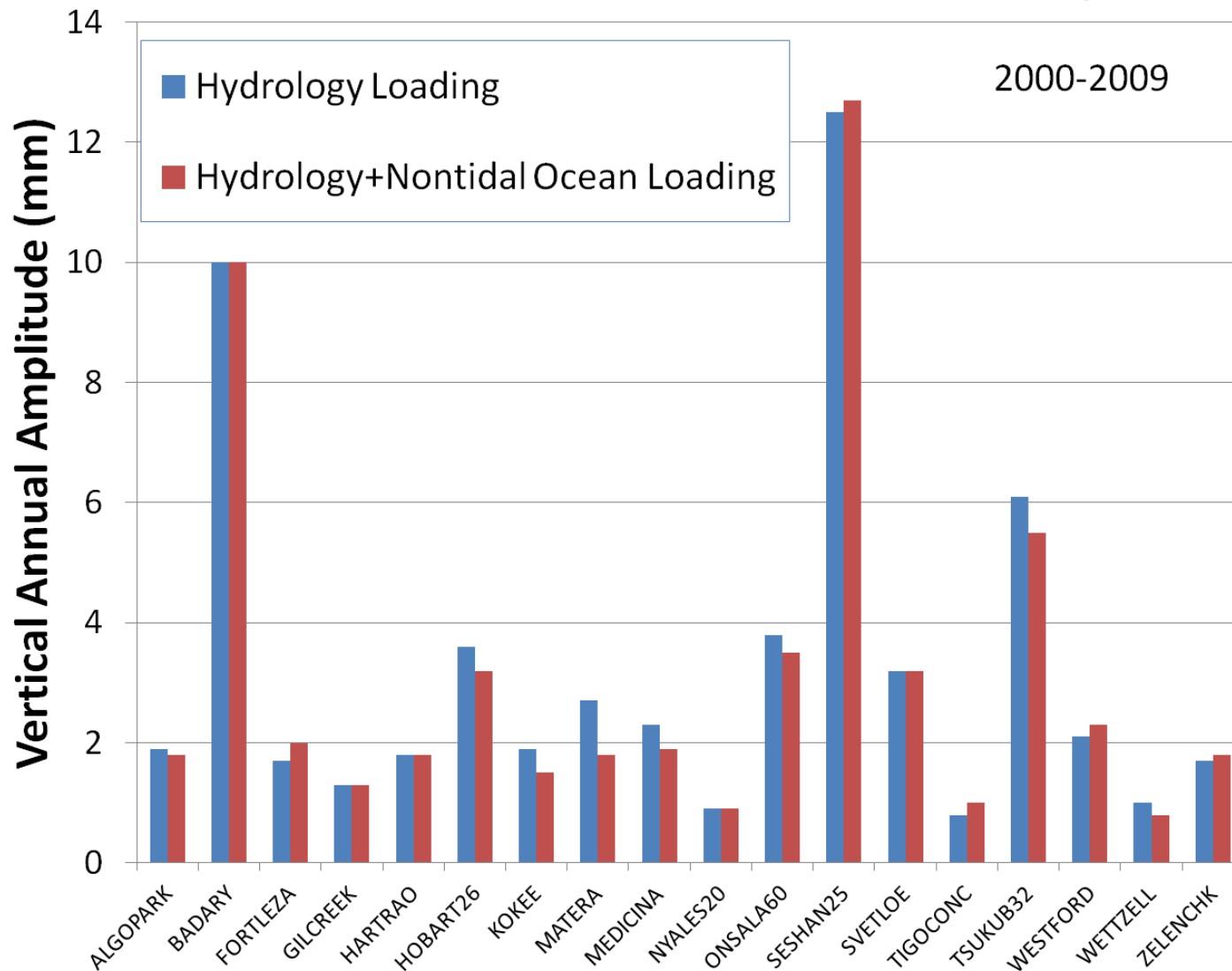


Nontidal Ocean Loading



Nontidal Ocean Loading

R1+R4 operational networks



Hydrology Loading

- GLDAS NOAH model since 1979, updated when data is available
- Monthly series for 170 VLBI stations
- 1x1 degree gridded map with loading series for each lattice point
- <http://lacerta.gsfc.nasa.gov/hydlo/>

Nontidal Ocean Loading

- JPL ECCO model since 1993, updated when data is available
- 12-hour resolution series for 170 VLBI stations
- 1x1 degree gridded map will be generated in future
- <http://lacerta.gsfc.nasa.gov/oclo/>

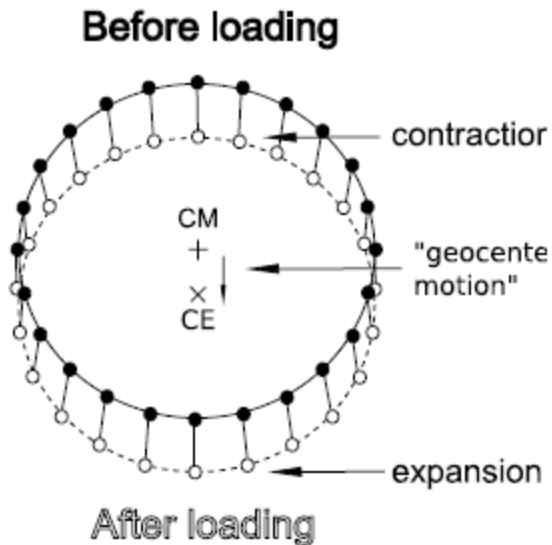
Atmospheric Pressure Loading

- Maintain Petrov-Boy series
- NCEP Reanalysis since 1979, updated when data is available
- 6-hour series for 824 VLBI+GPS+SLR sites
- 2.5x2.5 degree gridded map with loading series for each lattice point
- http://lacerta.gsfc.nasa.gov/aplo_eph/

Blewitt et al. (2001), Trupin et al. (1992): Surface mass load transport =>

- 1) Displacement of the geocenter
- 2) Deg-1 deformation of the Earth's surface

Lavallee and Blewitt (2002): Correlation between VLBI baseline length measurements and deg-1 deformation determined from GPS



- VLBI is not directly sensitive to the geocenter since it is not a satellite technique
- Indirectly sensitive via deg-1 deformation

From Lavallee, 2006

Degree-1 Loading

Displacement of CM relative to CE: CM=center of mass solid Earth+load
CE=center of mass solid Earth

$$\Delta \mathbf{r}_{\text{CM}} = \frac{M_L \Delta \mathbf{r}_L}{M_E} = \frac{\mathbf{m}}{M_E} \quad \mathbf{m} \equiv M_L \Delta \mathbf{r}_L$$

M_L = transported load mass $\Delta \mathbf{r}_L$ = center of mass of M_L in CE

Load moment vector $\mathbf{m} \sim$ deg-1 coefficients of the surface mass density

$$\mathbf{m} = \frac{4\pi R^3}{3} (\sigma_{11c}, \sigma_{11s}, \sigma_{10c})$$

Deg-1 displacement in CF (center of figure frame) is

$$\Delta \mathbf{s} = \mathbf{G}^T \text{diag}[h'_1, l'_1, l'_1] \mathbf{G} \frac{\mathbf{m}}{M_E} \quad \begin{array}{l} \mathbf{G} \text{ is topocentric } \rightarrow \text{ geocentric rotation} \\ h'_1, l'_1 \text{ are deg-1 Love numbers in CF} \end{array}$$

Estimate \mathbf{m} from VLBI data. Infer geocenter motion $\Delta \mathbf{r}_{\text{CM}}$.

Geocenter Annual Motion



	X		Y		Z	
	Amp (mm)	Phase (day)	Amp (mm)	Phase (day)	Amp (mm)	Phase (day)
VLBI 1985-2002	4.3 ± 0.8	10 ± 12	5.0 ± 0.8	202 ± 10	5.5 ± 0.8	70 ± 9
VLBI 1985-2010	9 ± 0.6	36 ± 9	5.5 ± 0.6	230 ± 8	6.5 ± 0.6	76 ± 7
SLR 1993-2002 Moore & Wang (2003)	3.5 ± 0.6	26 ± 10	4.3 ± 0.6	303 ± 8	4.6 ± 0.6	33 ± 7
SLR 2002-2010 Cheng et al. (2010)	3.2 ± 0.4	31 ± 5	2.6 ± 0.4	305 ± 5	4.3 ± 0.3	31 ± 5

- VLBI estimates subject to aliasing from higher spherical harmonics
- VLBI global coverage is lacking especially in the southern hemisphere
- Remaining unmodeled annual variation in VLBI

Summary



- Annual site displacement amplitudes are reduced with the VMF1 mapping functions + thermal deformation model + loading corrections
- Application of hydrology loading and nontidal ocean loading reduce the residual site position scatter
- Applying the loading corrections + thermal deformation + VMF1 reduces the annual amplitude of the VLBI reference frame scale from 0.54 ppb to 0.08 ppb
- Estimation of the degree-1 components of surface deformation from VLBI data imply geocenter annual amplitudes that are generally too large compared to those determined from SLR
- In future work we will try to limit aliasing of higher degree terms into the VLBI estimates by applying displacements ($\text{deg} > 1$) derived from GRACE or geophysical models (ocean, hydrology, atmosphere)